WEIGHTED MATRIX STRUCTURAL ADJUSTMENT IMPROPER LINEAR PROGRAMMING PROBLEMS OF THE 1ST KIND¹

V.I. Erohin, M.N. Hvostov

St. Petersburg State Technological Institute (Technical University), St. Petersburg, Borisoglebsk State Pedagogical Institute, Borisoglebsk e-mail: erohin v i@mail.ru, hvostoff@inbox.ru

The report, in the continuation of research initiated in [1], the problem of P matrix correction of improper linear programming (LP) of the 1st kind of the minimum weighted Euclidean norm in the case where the elements of the augmented matrix [A - b] coefficients of its limitations divided into a plurality of adjustable $[K^+ k^+]$ and uncorrectable $[K^- k^-]$ elements.

Theorem. If the problem P has a solution, then the desired vectors and matrices can be constructed by direct formulas that depend on the solutions (soluble under these conditions) unconstrained minimization problem.

$$\Phi(\tilde{x}) = \sum_{i=1}^{m} \frac{\left(b - A\left(\operatorname{diag}(\tilde{x})\tilde{x}\right)\right)_{i}^{2} \cdot \left|s\left(\begin{bmatrix}\operatorname{diag}(\tilde{x})\tilde{x}\\1\end{bmatrix}, \begin{bmatrix}\mathcal{H}_{i*}^{\top}\\\chi_{i}\end{bmatrix}\right) \cdot \operatorname{diag}\left(\begin{bmatrix}\mathcal{W}_{i*}^{\top}\\\omega_{i}\end{bmatrix}\right)\right|^{2}}{\left(s^{\top}\left(\begin{bmatrix}\operatorname{diag}(\tilde{x})\tilde{x}\\1\end{bmatrix}, \begin{bmatrix}\mathcal{H}_{i*}^{\top}\\\chi_{i}\end{bmatrix}\right) \cdot s\left(\begin{bmatrix}\operatorname{diag}(\tilde{x})\tilde{x}\\1\end{bmatrix}, \begin{bmatrix}\mathcal{H}_{i*}^{\top}\\\chi_{i}\end{bmatrix}\right)\right)^{2}} \to \min,$$

where the coefficients $\begin{bmatrix} \mathcal{W}_{i*}^{\mathsf{T}} \\ \omega_i \end{bmatrix}$ determine the weight of each *i*-th row correction matrix $\begin{bmatrix} H & -h \end{bmatrix}$ in the objective function, \mathcal{H}_{i*} - *i*-th row of the matrix \mathcal{H} , $s(p,q) = (s(p,q)_i) \begin{vmatrix} s(p,q)_i = p_i, & \text{if } q_i \neq 0 \\ s(p,q)_i = 0, & \text{if } q_i = 0 \end{vmatrix}$, $\mathcal{H} = (\mathcal{H}_{ij}) \begin{vmatrix} \mathcal{H}_{i,j} = 1, & \text{if } \{i,j\} \in \mathbf{K}^+ \\ \mathcal{H}_{i,j} = 0, & \text{if } \{i,j\} \in \mathbf{K}^- \end{vmatrix}$, $\chi = (\chi_i) \begin{vmatrix} \chi_i = 1, & \text{if } \{i\} \in \mathbf{k}^+ \\ \chi_i = 0, & \text{if } \{i\} \in \mathbf{k}^- \end{vmatrix}$.

Analytical formulas for the gradient of this function are given [2]. Computational procedure of minimization with the use of an algorithm Broyden-Fletcher-Goldfarb-Shanno is implemented. Results of model problems of middle dimension with sparse matrix coefficients from the catalog "lp/infeas" storage Netlib, illustrating the convergence of the argument and the objective function and the distribution of elements on the amendments are given.

REFERENCES

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¹Supported by an RFBR (Project N 14-01-31318)